

Design methods for HSS cross-sections

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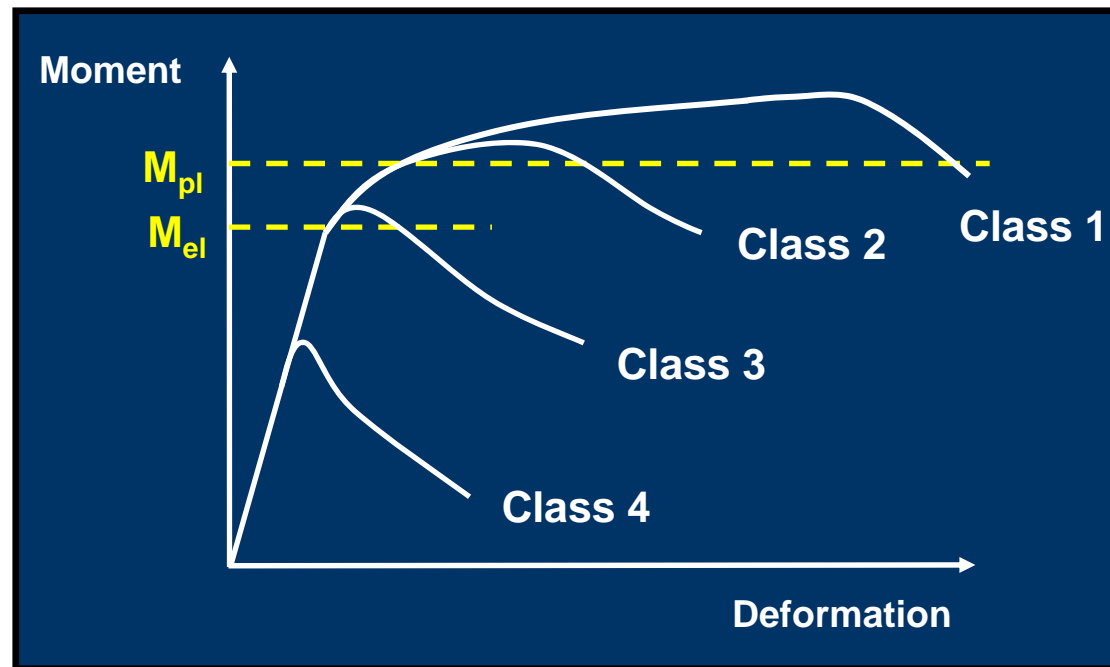
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Overview

1. Experimental programme on HSS hollow sections
 - Material tests
 - Stub column tests
 - Beam tests
 - Combined axial load and bending tests
2. Cross-section design of HSS hollow sections
 - Slenderness limits for internal elements in compression
 - Slenderness limits for internal elements in bending
 - Interaction curve for combined axial load and bending
3. Concluding remarks

Cross-section design: Eurocode 3 approach

- Local buckling is considered through the process of cross-section classification:
- Four Classes of behavior based on:
 - Moment capacity;
 - Rotation capacity and
 - Compression capacity of the cross-section



Cross-section design: Eurocode 3 design approach

Which cross-section classification does a section fall into?

- Geometric properties of the section
- Material properties (f_y) of the section

Single slenderness parameter $c/t.\epsilon$ ratio ($\epsilon = \sqrt{235/f_y}$) c_w

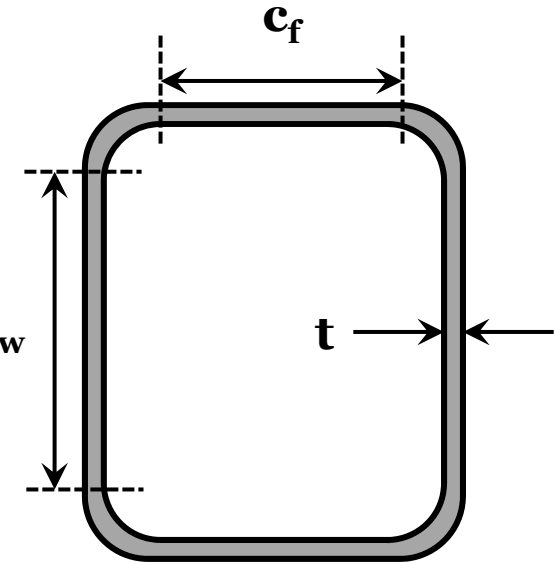


Table 5.2 (sheet 1 of 3): Maximum width-to-thickness ratios for compression parts

Internal compression parts	
Class	Part subject to bending
1	$c/t \leq 72\epsilon$
2	$c/t \leq 83\epsilon$
3	$c/t \leq 124\epsilon$

Table 5.2 (sheet 2 of 3): Maximum width-to-thickness ratios for compression parts

Class	Part subject to bending	Rolled sections		Welded sections	
		Part subject to compression	Part subject to bending and compression	Tip in compression	Tip in tension
1	$c/t \leq 72\epsilon$	$c/t \leq 33\epsilon$	$c/t \leq 9\epsilon$	$c/t \leq \frac{9\epsilon}{\alpha\sqrt{\alpha}}$	$c/t \leq \frac{9\epsilon}{\alpha\sqrt{\alpha}}$
2	$c/t \leq 83\epsilon$	$c/t \leq 38\epsilon$	$c/t \leq 10\epsilon$	$c/t \leq \frac{10\epsilon}{\alpha}$	$c/t \leq \frac{10\epsilon}{\alpha\sqrt{\alpha}}$
3	$c/t \leq 124\epsilon$				

EC3 $c/t.\epsilon$ ratios were derived based on tests on steel sections with $f_y < 460 \text{ N/mm}^2$

Need to be verified for high strength steel with $460 \text{ N/mm}^2 < f_y < 1100 \text{ N/mm}^2$

*) $\psi \leq -1$ applies where either the compression stress $\sigma \leq f_c$ or the tensile strain $\epsilon_y \geq f_t/E$

Experimental programme

Investigated cross-sections

- Tubular SHS and RHS
- Grades S460 and S690
- S460 hot-rolled and normalised
- S690 hot-rolled and quenched and tempered
- Specimens were provided by Vallourec

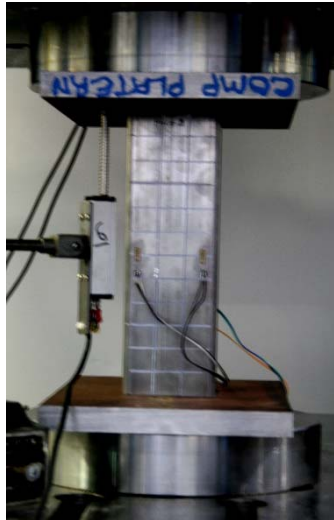


Grade	Cross-section
S460	SHS 50×50×5
	SHS 50×50×4
	SHS 100×100×5
	SHS 90×90×3.6
	RHS 100×50×6.3
	RHS 100×50×4.5
S690	SHS 50×50×5
	SHS 100×100×5.6
	SHS 90×90×5.6
	RHS 100×50×6.3
	RHS 100×50×5.6

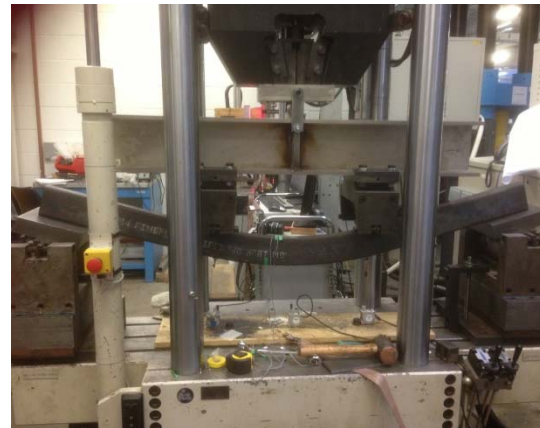
Experimental programme

Summary of cross-section tests:

- 11 concentrically loaded stub column tests
- In-plane bending tests (11 3-PB and 11 4-PB configurations)
- 12 eccentrically loaded stub column tests
- Tensile coupon (29 flats and 11 corners) and compressive coupon (11 flats) tests



Stub column test



Bending test



Combined loading tests

Cross-section design

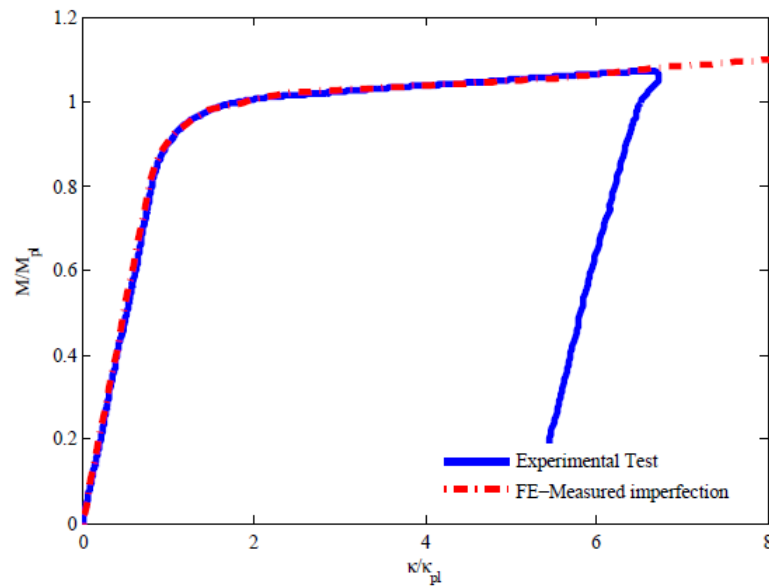
Finite Element Modelling

- FE models of stub columns and beams were developed in ABAQUS
- Models were validated against the test results
 - Full loading history and failure modes well predicted
- Parametric studies were conducted, varying:
 - Material grade;
 - Moment gradient and
 - Cross-section aspect ratio (h/b)

Cross-section design

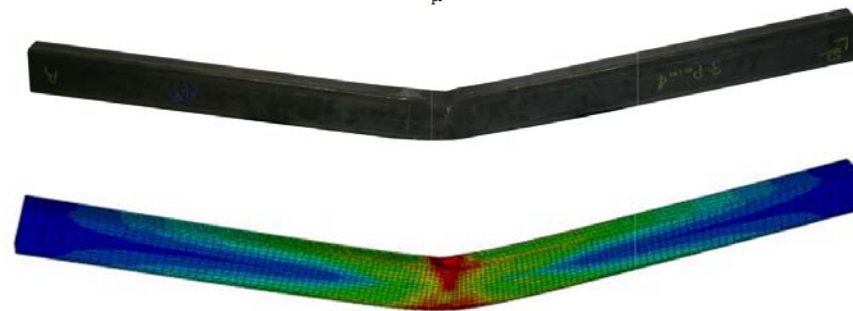
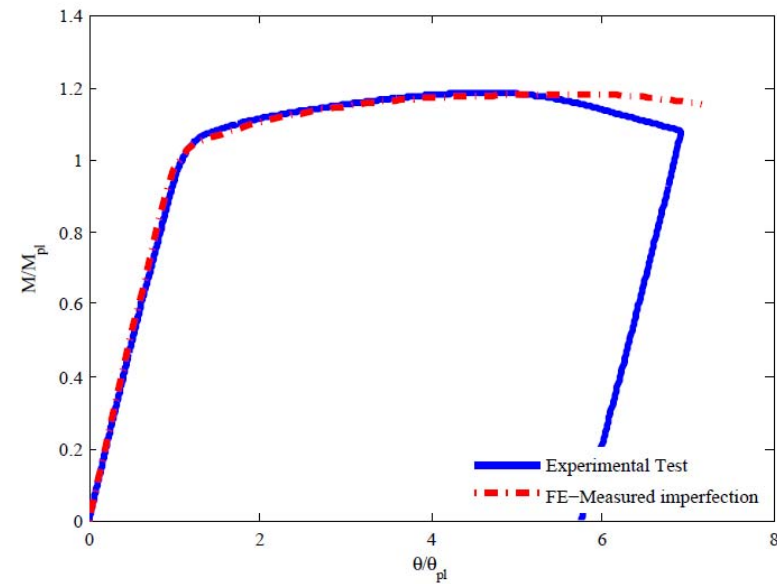
Finite Element Modelling - validation

4PB: Moment-curvature response



Four-point bending

3PB: Moment-rotation response

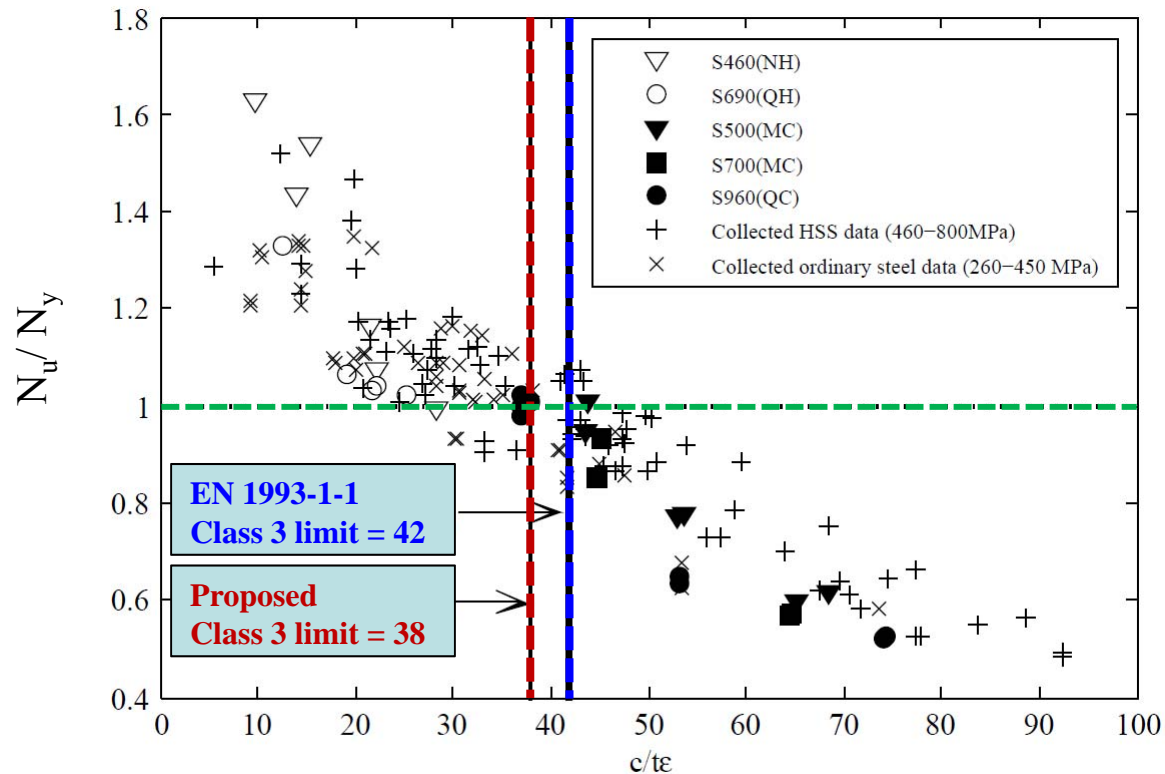


Three-point bending

Cross-section design

Class 3 ($c/t.\epsilon$) limit for internal elements in compression:

Max load N_u normalised by yield load N_y

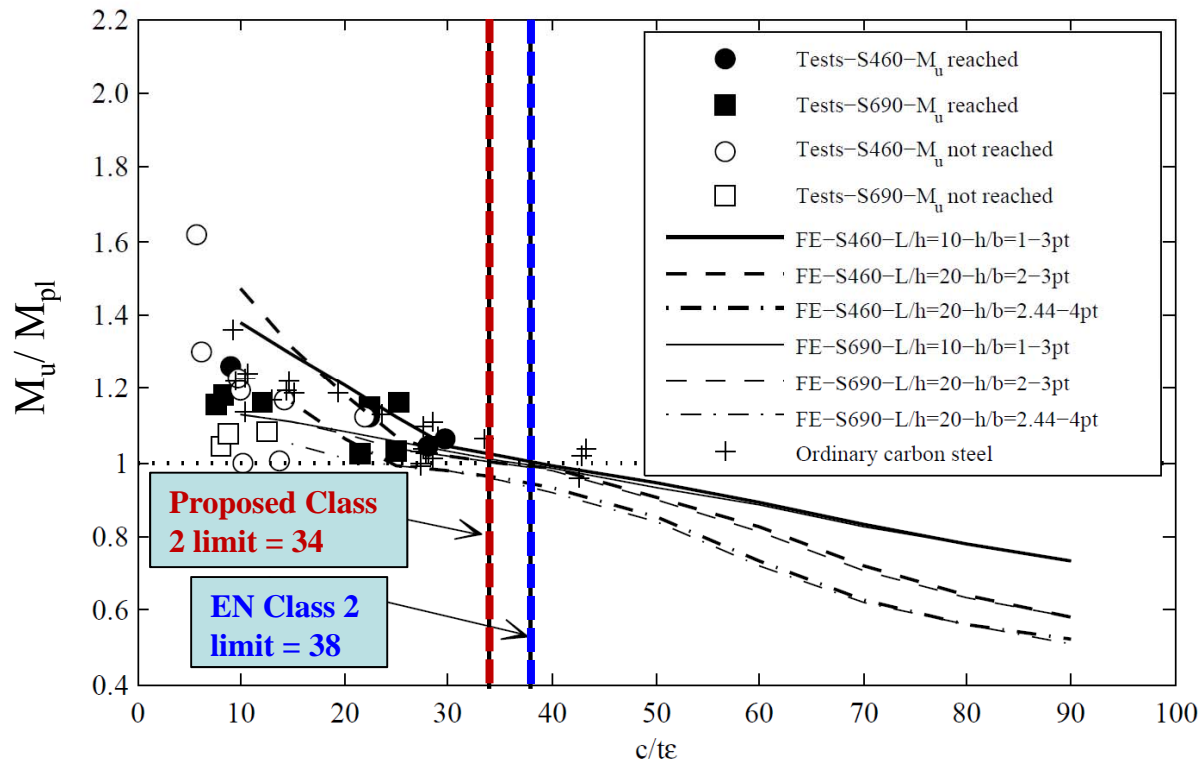


- EN 1993-1-1 → 42 unsafe
- SC3 Evolution group for ordinary carbon steel → 38 more appropriate

Cross-section design

Class 2 ($c/t.\varepsilon$) limit for internal elements in compression:

Max moment M_u normalised by plastic moment capacity M_{pl}

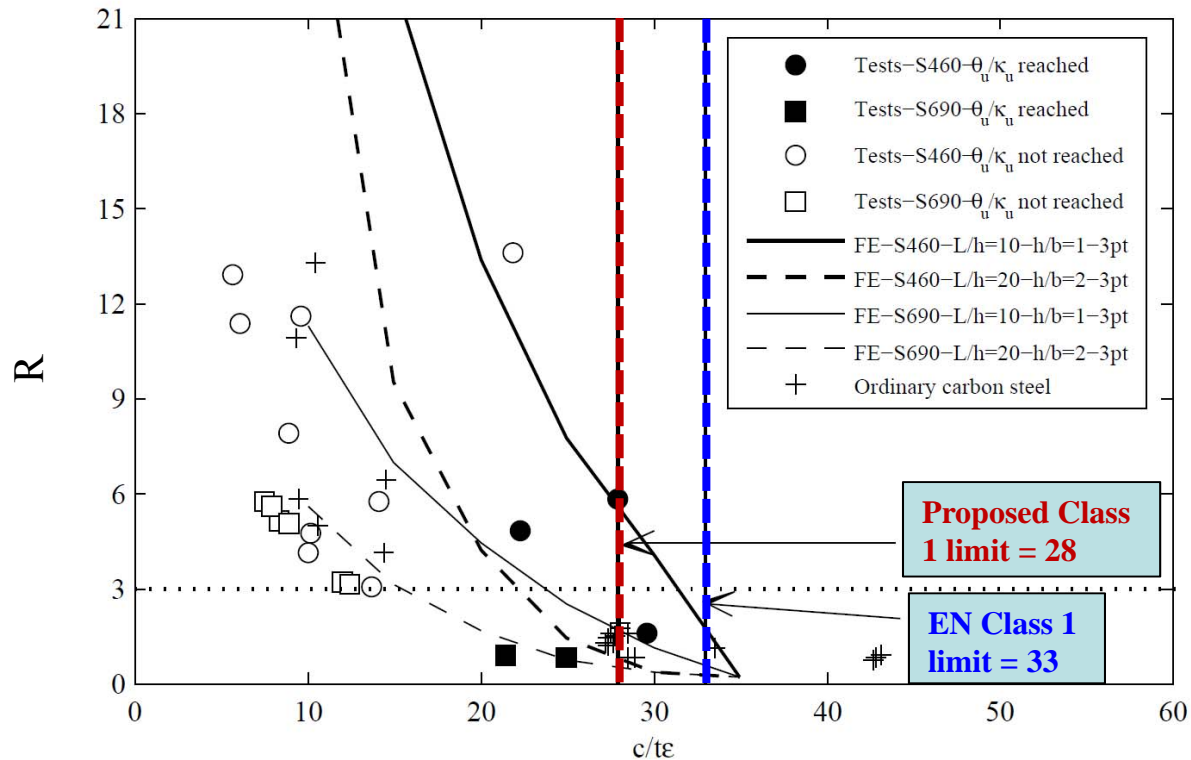


- EN 1993-1-1 → **38** too optimistic
- SC3 Evolution group for ordinary carbon steel → **34** more appropriate

Cross-section design

Class 1 ($c/t.\epsilon$) limit for internal elements in compression:

Max rotation capacity R



- EN 1993-1-1 → **33** too optimistic
- SC3 Evolution group for ordinary carbon steel → **28** more appropriate

Cross-section design

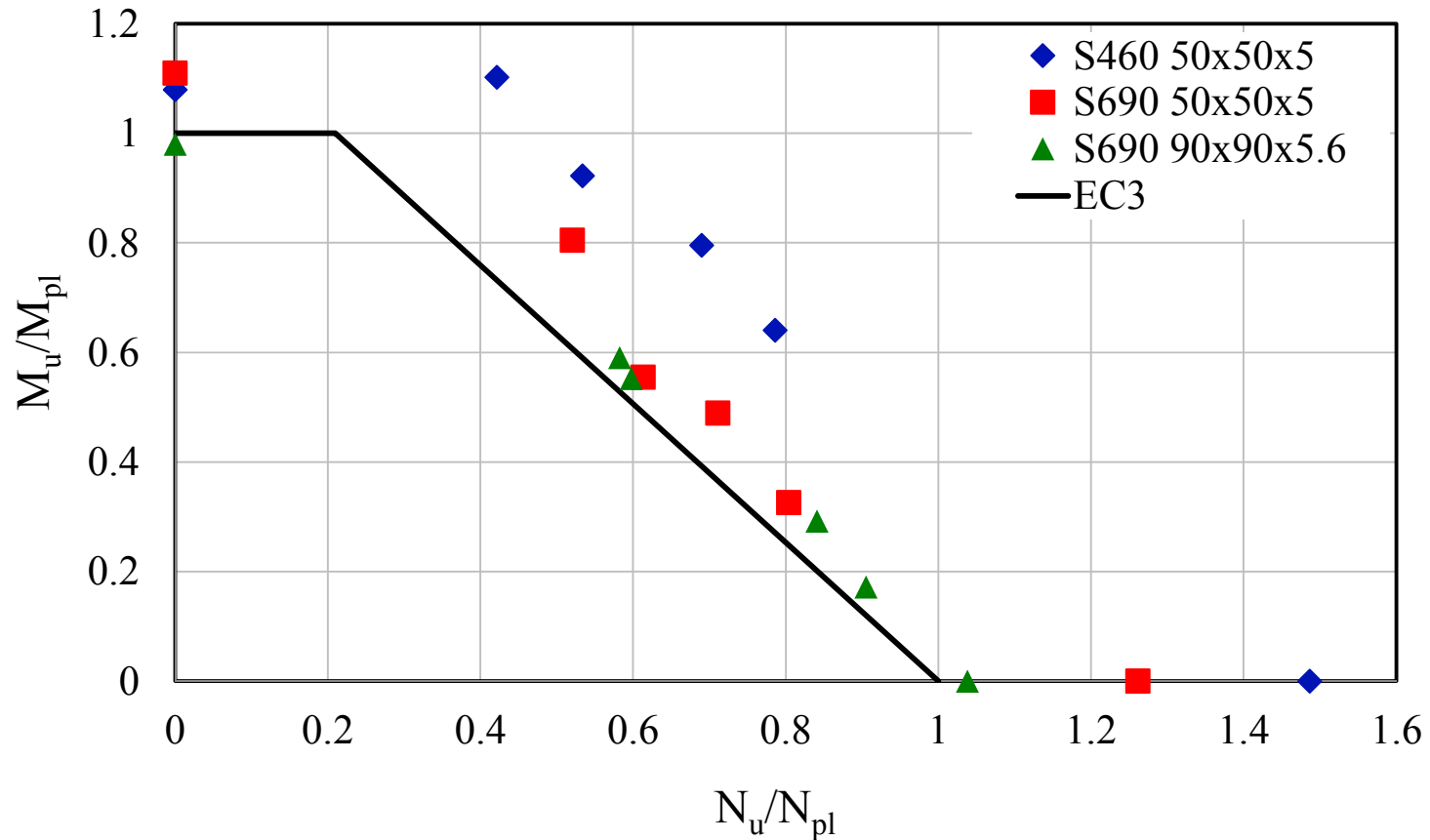
Summary of $(c/t.\epsilon)$ slenderness limits for:

- Internal elements in compressions
- Internal elements in bending

Element Type	Class 1	Class 2	Class 3
Internal element in compression	28	34	38
Internal element in bending	72	83	121

Cross-section design

Moment axial load interaction curve based on test results



- Current EC3 interaction curve is also suitable for high strength steel hollow sections

Concluding remarks

- Experimental programme on HSS hollow sections
- Cross-section classification limits for hollow sections
 - Internal elements in compression
 - Internal elements in bending
- Interaction curve for cross-sections under combined axial load and bending

Design methods for HSS cross-sections

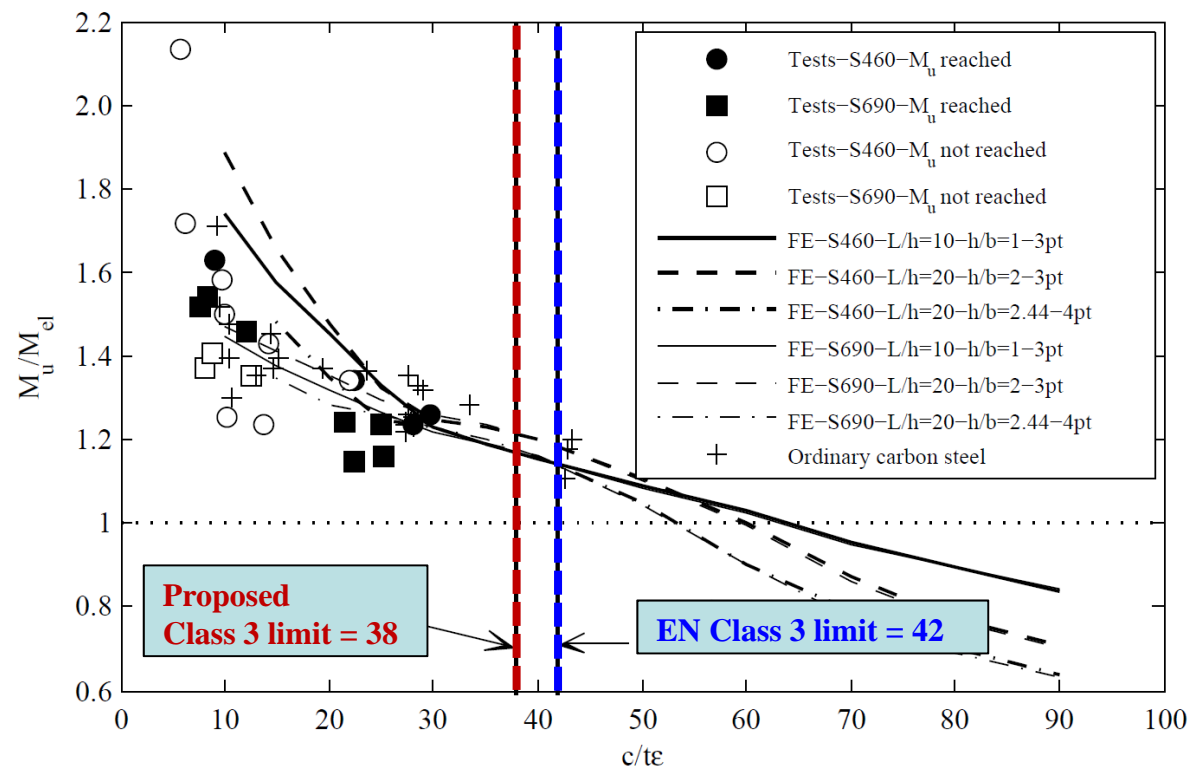
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Cross-section design

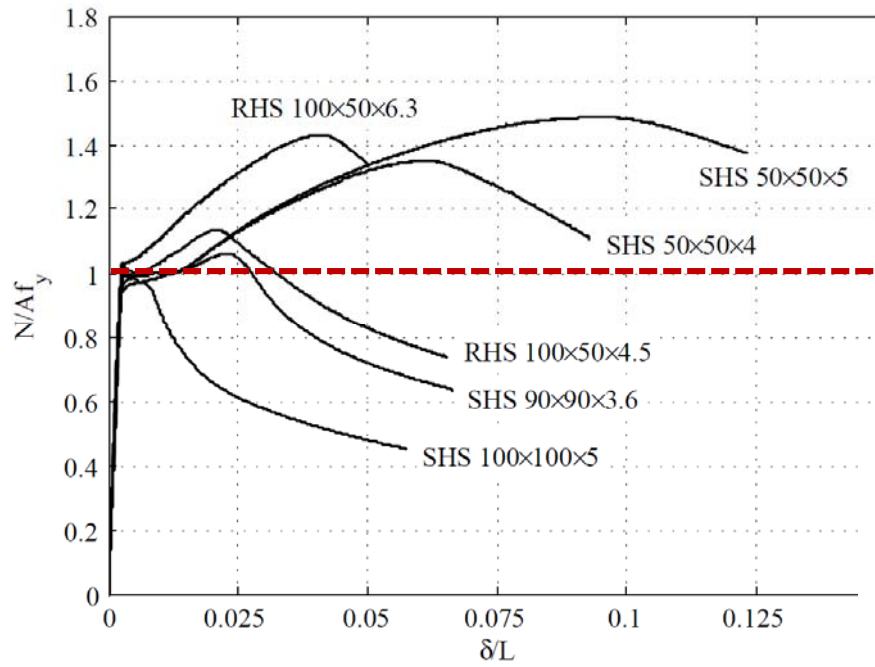
Class 3 ($c/t, \varepsilon$) limit based on bending test results:

Max moment M_u normalised by elastic moment capacity M_{el}

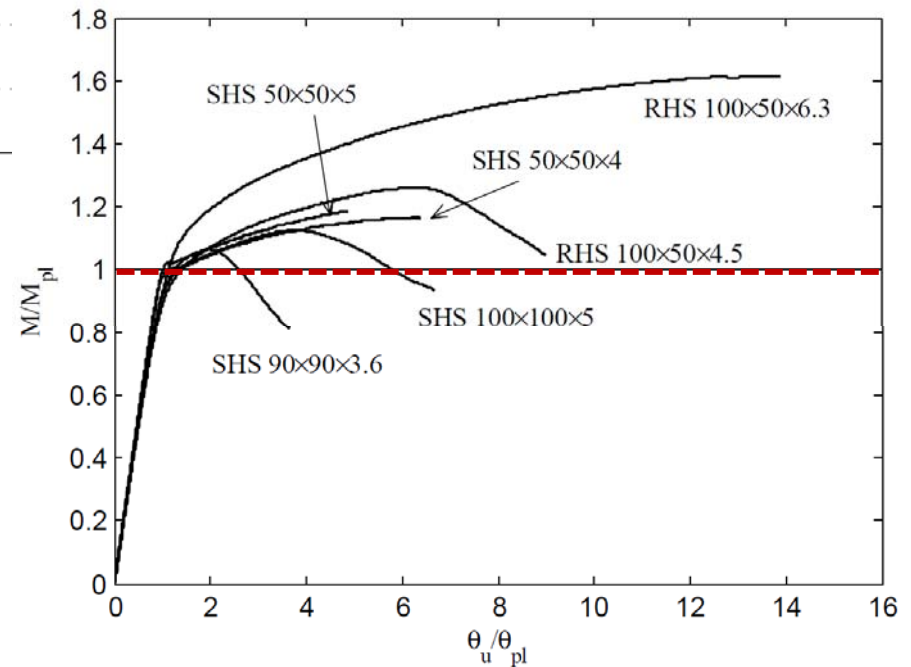


The Continuous Strength Method (CSM)

HSS sections capable of reaching $N_u > N_y$



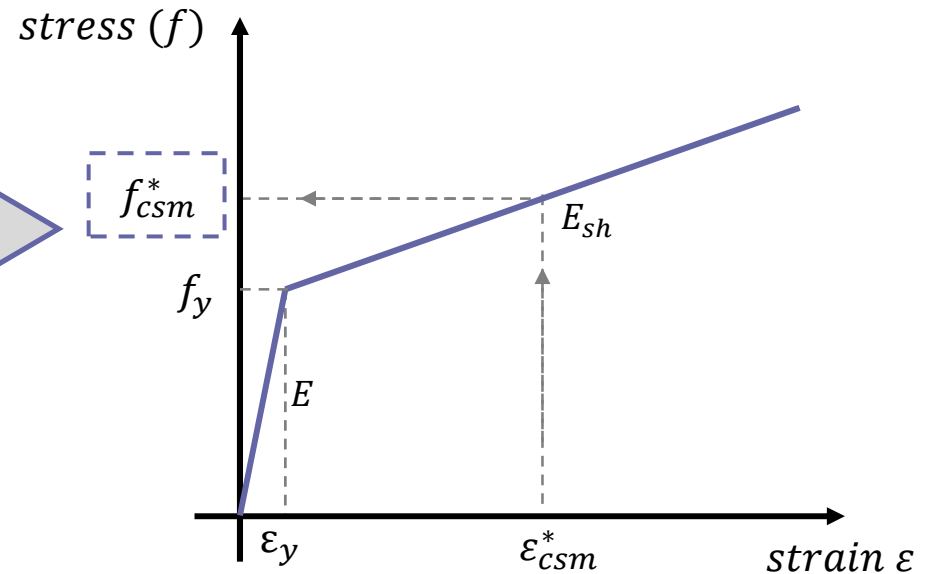
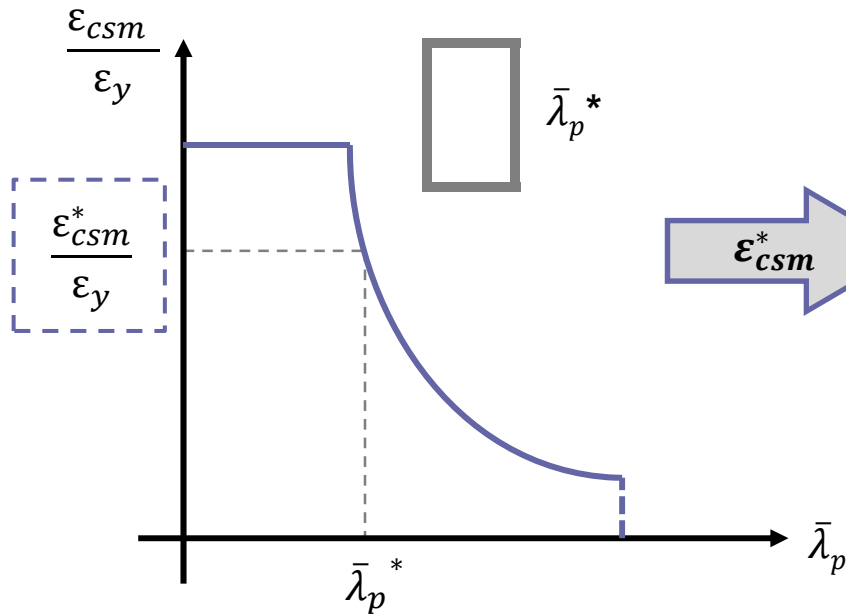
HSS sections capable of reaching $M_u > M_{pl}$



The Continuous Strength Method (CSM)

Base curve

Material model



Cross-section compression resistance

Cross-section bending resistance

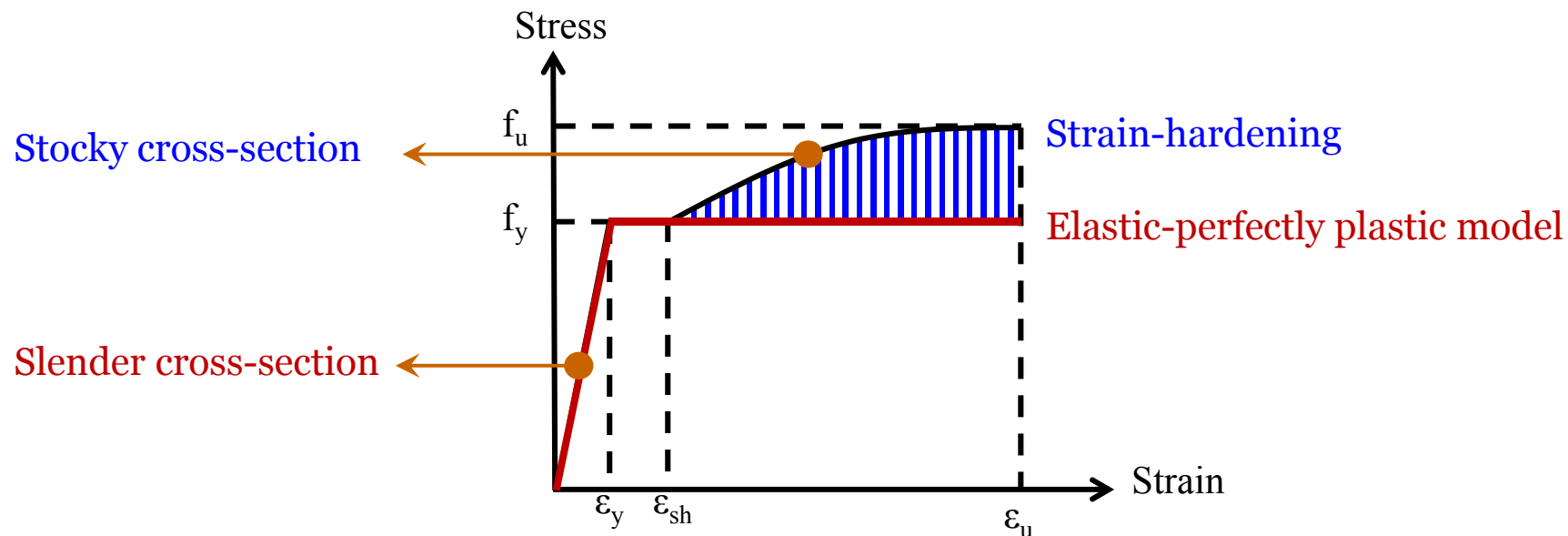
$$N_{csm} = Af_{csm} = A[f_y + (\varepsilon_{csm} - \varepsilon_y)E_{sh}]$$

$$\frac{M_{csm}}{M_{pl}} = 1 + \frac{E_{sh}}{E} \frac{W_{el}}{W_{pl}} \left(\frac{\varepsilon_{csm}}{\varepsilon_y} - 1 \right) - \left(1 - \frac{W_{el}}{W_{pl}} \right) \left(\frac{\varepsilon_{csm}}{\varepsilon_y} \right)^{-2}$$

The Continuous Strength Method (CSM)

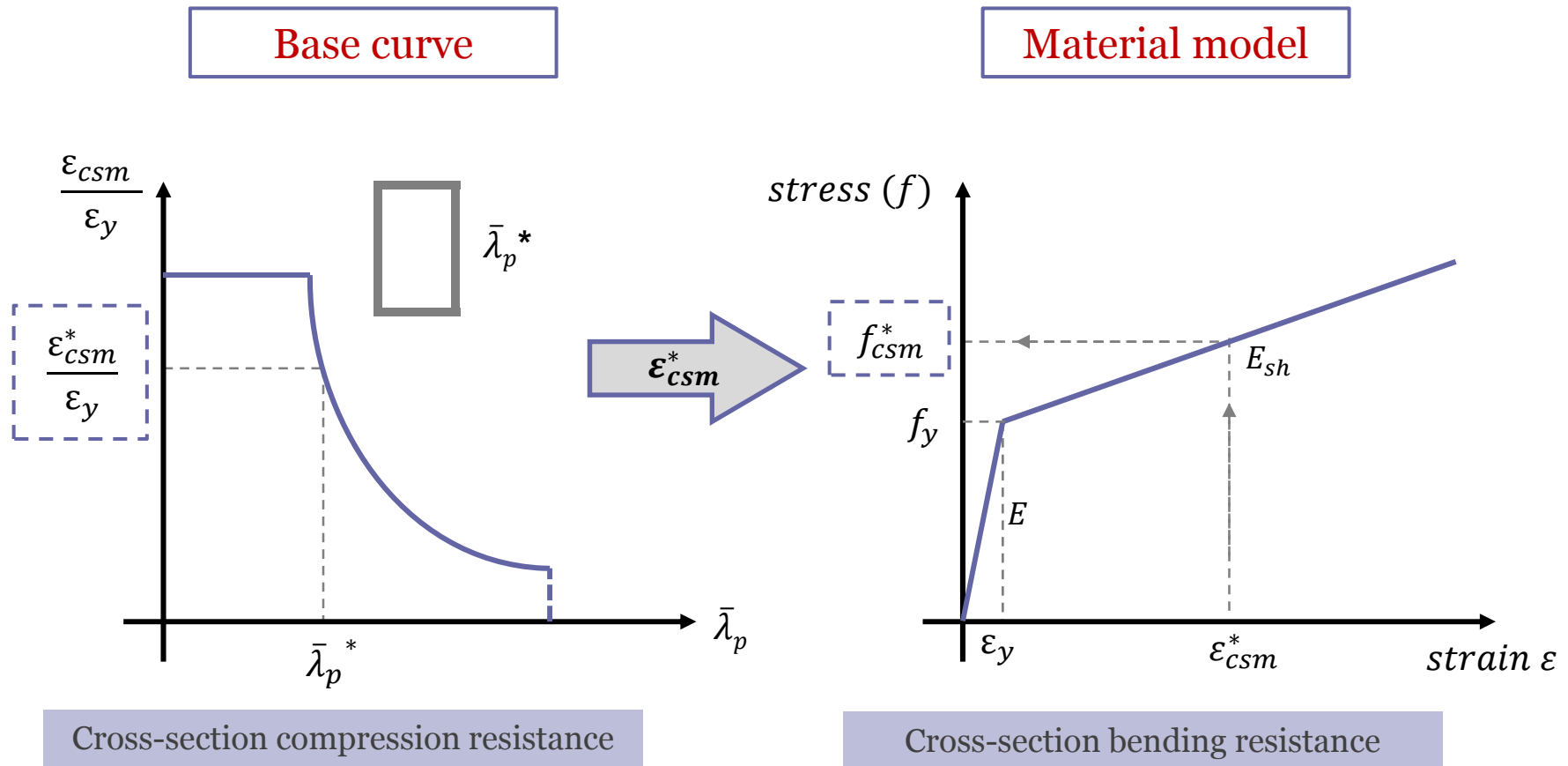
Background:

- Drawbacks of current EC3 classification system:
 - Limits the compression resistance to yield load N_y (Af_y)
 - Limits the cross-section bending resistance to plastic moment M_{pl} ($W_{pl}f_y$)



- Continuous Strength Method developed for the design of:
 - Stocky cross-sections (low $c/t.\epsilon$ ratio) which are capable of reaching $N_u > N_y$
 - Stocky cross-sections (low $c/t.\epsilon$ ratio) which are capable of reaching $M_u > M_{pl}$

The Continuous Strength Method (CSM)

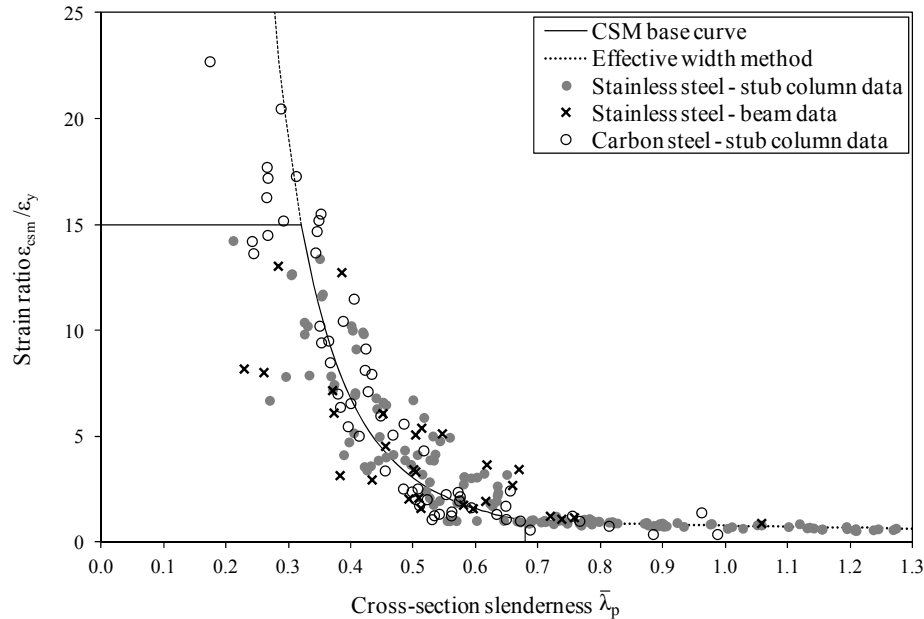


$$N_{csm} = Af_{csm} = A[f_y + (\varepsilon_{csm} - \varepsilon_y)E_{sh}]$$

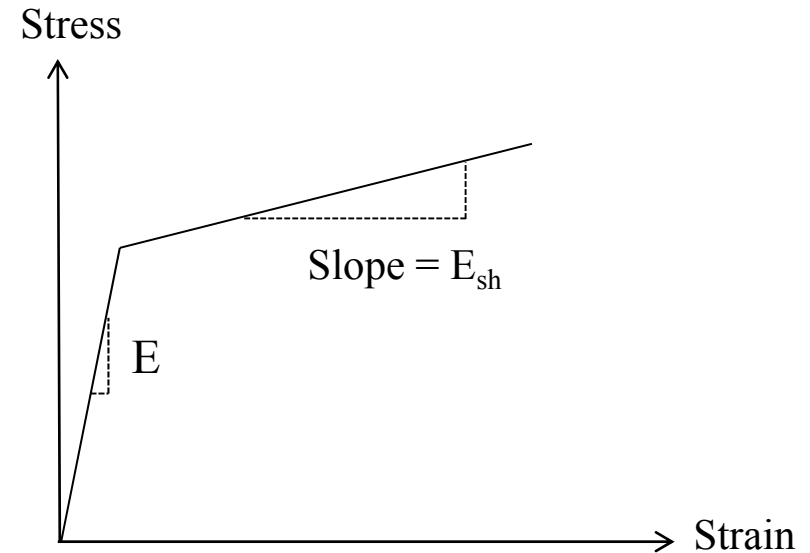
$$\frac{M_{csm}}{M_{pl}} = 1 + \frac{E_{sh}}{E} \frac{W_{el}}{W_{pl}} \left(\frac{\varepsilon_{csm}}{\varepsilon_y} - 1 \right) - \left(1 - \frac{W_{el}}{W_{pl}} \right) \left(\frac{\varepsilon_{csm}}{\varepsilon_y} \right)^{-2}$$

The Continuous Strength Method (CSM)

Base curve



Material model



$$\frac{\epsilon_{csm}}{\epsilon_y} = \frac{0.25}{\bar{\lambda}_p^{3.6}} \quad \text{but} \quad \frac{\epsilon_{csm}}{\epsilon_y} < \min\left(15, 0.45 \frac{\epsilon_u}{\epsilon_y}\right)$$

$$E_{sh} = \frac{f_u - f_y}{0.5\epsilon_u - \epsilon_{sh}} \quad \text{if} \quad \frac{\epsilon_{sh}}{\epsilon_u} < 0.5 \quad \text{else,} \quad E_{sh} = 0$$

Initial analysis of the results has shown that:

- CSM provides more accurate estimation of cross-section capacity
- Especially for HSS grades with higher f_u/f_y ratio